



## 10.4 Archimedes' Principle

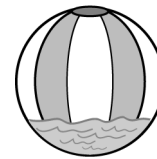
**READ**


More than 2,000 years ago, Archimedes discovered the relationship between buoyant force and how much fluid is displaced by an object. **Archimedes' principle** states:

**The buoyant force acting on an object in a fluid is equal to the weight of the fluid displaced by the object.**

We can practice figuring out the buoyant force using a beach ball and a big tub of water. Our beach ball has a volume of  $14,130 \text{ cm}^3$ . The weight of the beach ball in air is  $1.5 \text{ N}$ .

If you put the beach ball into the water and don't push down on it, you'll see that the beach ball floats on top of the water by itself. Only a small part of the beach ball is underwater. Measuring the volume of the beach ball that is under water, we find it is  $153 \text{ cm}^3$ . Knowing that  $1 \text{ cm}^3$  of water has a mass of  $1 \text{ g}$ , you can calculate the weight of the water displaced by the beach ball.



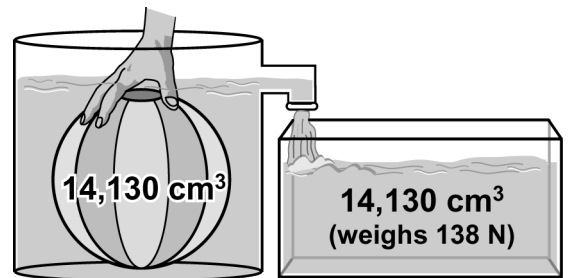
water displaced  
by  
floating ball  
 $153 \text{ cm}^3$   
 $1.5 \text{ N}$

$$153 \text{ cm}^3 \text{ of water} = 153 \text{ grams} = 0.153 \text{ kg}$$

$$\text{weight} = \text{mass} \times \text{force of gravity per kg} = (0.153 \text{ kg}) \times 9.8 \text{ N/kg} = 1.5 \text{ N}$$

According to Archimedes principle, the buoyant force acting on the beach ball equals the weight of the water displaced by the beach ball. Since the beach ball is floating in equilibrium, the weight of the ball pushing down must equal the buoyant force pushing up on the ball. We just showed this to be true for our beach ball.

Have you ever tried to hold a beach ball underwater? It takes a lot of effort! That is because as you submerge more of the beach ball, the more the buoyant force acting on the ball pushes it up. Let's calculate the buoyant force on our beach ball if we push it all the way under the water. Completely submerged, the beach ball displaces  $14,130 \text{ cm}^3$  of water. Archimedes principle tells us that the buoyant force on the ball is equal to the weight of that water:



$$14,130 \text{ cm}^3 \text{ of water} = 14,130 \text{ grams} = 14.13 \text{ kg}$$

$$\text{weight} = \text{mass} \times \text{force of gravity per kg} = (14.13 \text{ kg}) \times 9.8 \text{ N/kg} = 138 \text{ N}$$

If the buoyant force is pushing up with  $138 \text{ N}$ , and the weight of the ball is only  $1.5 \text{ N}$ , your hand pushing down on the ball supplies the rest of the force,  $136.5 \text{ N}$ .

### EXAMPLE

- A  $10\text{-cm}^3$  block of lead weighs  $1.1 \text{ N}$ . The lead is placed in a tank of water. One  $\text{cm}^3$  of water weighs  $0.0098 \text{ N}$ . What is the buoyant force on the block of lead?

**Solution:**

The lead displaces  $10 \text{ cm}^3$  of water.  
 buoyant force = weight of water displaced  
 $10 \text{ cm}^3$  of water  $\times 0.0098 \text{ N/cm}^3 = 0.098 \text{ N}$


**PRACTICE**


1. A block of gold and a block of wood both have the same volume. If they are both submerged in water, which has the greater buoyant force acting on it?
2. A  $100\text{-cm}^3$  block of lead that weighs 11 N is carefully submerged in water. One  $\text{cm}^3$  of water weighs 0.0098 N.
  - a. What volume of water does the lead displace?
  - b. How much does that volume of water weigh?
  - c. What is the buoyant force on the lead?
  - d. Will the lead block sink or float in the water?
3. The same  $100\text{-cm}^3$  lead block is carefully submerged in a container of mercury. One  $\text{cm}^3$  of mercury weighs 0.13 N.
  - a. What volume of mercury is displaced?
  - b. How much does that volume of mercury weigh?
  - c. What is the buoyant force on the lead?
  - d. Will the lead block sink or float in the mercury?
4. According to problems 2 and 3, does an object's density have anything to do with whether or not it will float in a particular liquid? Justify your answer.
5. Based on the table of densities, explain whether the object would float or sink in the following situations:

material	density ( $\text{g/ cm}^3$ )
gasoline	0.7
gold	19.3
lead	11.3
mercury	13.6
molasses	1.37
paraffin	0.87
platinum	21.4

- a. A block of solid paraffin (wax) in molasses.
- b. A bar of gold in mercury.
- c. A piece of platinum in gasoline.
- d. A block of paraffin in gasoline.